

1) RAW DATA (NO TABLE)

(X) Ages: 7, 4, 3, 6, 6, 5

X	X <sup>2</sup>	
7	49	MEAN = $\frac{\sum x}{n} = \frac{31}{6} = 5.167$
4	16	
3	9	STANDARD DEVIATION = $\sqrt{\frac{\sum x^2}{n} - \left(\frac{\sum x}{n}\right)^2}$
6	36	
6	36	
5	25	= $\sqrt{\frac{171}{6} - \left(\frac{31}{6}\right)^2} = 1.3437$
$\sum x = 31$	$\sum x^2 = 171$	VARIANCE = (SD) <sup>2</sup> = (1.3437) <sup>2</sup>
		= 1.8055

2) FREQUENCY DISTRIBUTION TABLE (SINGLE VALUE TABLE)

Name's Break till 5:40

X <sup>2</sup>	0	1	4	9	
x/mark	0	1	2	3	
f	10	5	25	60	$\sum f = 100$
fx	0	5	50	180	$\sum fx = 235$
fx <sup>2</sup>	0	5	100	540	$\sum fx^2 = 645$

$$\text{MEAN} = \frac{\sum fx}{\sum f} = \frac{235}{100} = 2.35$$

$$\text{STANDARD DEVIATION} = \sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f}\right)^2} = \sqrt{\frac{645}{100} - \left(\frac{235}{100}\right)^2}$$

$$= 0.9630$$

$$\text{VARIANCE} = (\text{SD})^2 = (0.9630)^2 = 0.9275.$$

### 3) FREQUENCY DISTRIBUTION TABLE ( RANGE TABLE )

$x^2$	25	625	2025	
Mid(x)	5	25	45	
x/marks	$0 < x \leq 10$	$10 < x \leq 40$	$40 < x \leq 50$	
f	40	30	10	$\Sigma f = 80$
fx	200	750	450	$\Sigma fx = 1400$
$fx^2$	1000	18750	20250	$\Sigma fx^2 = 40000$

$$\text{MEAN} = \frac{\Sigma fx}{\Sigma f} = \frac{1400}{80} = 17.5$$

$$\text{STANDARD DEVIATION} = \sqrt{\frac{\Sigma fx^2}{\Sigma f} - \left(\frac{\Sigma fx}{\Sigma f}\right)^2} = \sqrt{\frac{40000}{80} - \left(\frac{1400}{80}\right)^2}$$
$$= 13.9194$$

$$\text{VARIANCE} = (\text{SD})^2 = (13.9194)^2 = 193.75$$

$$\Sigma fx^2 \neq (\Sigma fx)^2$$

## PROBABILITY DISTRIBUTION

$X^2$	1	4	9	16	
$X$	1	2	3	4	
$P(x)$	0.2	$P=0.4$	0.1	0.3	$\sum P(x) = 1$
$x \cdot P(x)$	0.2	0.8	0.3	1.2	$E(X) = 2.5$
$x^2 \cdot P(x)$	0.2	1.6	0.9	4.8	$E(X^2) = 7.5$

$$1) \quad 0.2 + p + 0.1 + 0.3 = 1$$

$$p = 0.4$$

$$2) \quad \text{EXPECTED VALUE OF } X = \text{MEAN} = E(X)$$

$$E(X) = \sum [x \cdot P(x)] = 2.5$$

$$3) \quad \text{EXPECTED VALUE OF } X^2 = E(X^2) = \sum [x^2 \cdot P(x)] = 7.5$$

$$4) \quad \text{STANDARD DEVIATION} = \sqrt{E(X^2) - [E(X)]^2}$$

$$= \sqrt{7.5 - (2.5)^2}$$

$$= 1.180$$

$$5) \quad \text{VARIANCE} = (\text{SD})^2 = (1.180)^2 = 1.25$$

## STANDARD DEVIATION

RAW DATA

$$SD = \sqrt{\frac{\sum x^2}{n} - \left(\frac{\sum x}{n}\right)^2}$$

↓  
Mean

FREQUENCY  
TABLE

$$SD = \sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f}\right)^2}$$

↓  
Mean

PROBABILITY  
TABLES

$$SD = \sqrt{E(x^2) - [E(x)]^2}$$

↓  
Mean